(Rewrite) $[+3]$ For sets $A, B, C, D$, prove that $(A \cap C) \times(B \cap D) \subseteq(A \times B) \cap(C \times D)$.

