

If you are  $\text{\TeX}$ ing, the symbol “.” can be made by adding the command “`\newcommand{\st}{\,\hbox{\Huge .}\,}`” to the preamble and then called by “`\st`” when in math mode.

**(10 pts)**

(1) For each of the following propositions, write the negation without using  $\neg$

(a) [+2]  $\forall x \in \mathbb{Z} . \exists y \in \mathbb{Z} . x = 2y$

(b) [+2]  $\exists y \in \mathbb{R} . \forall x \in \mathbb{R} . y > x$

(c) [+2]  $\forall \epsilon > 0 . \exists \delta > 0 . (|x - x_0| < \delta) \Rightarrow (|y - y_0| < \epsilon)$

(2) Write the contrapositive of the following statements.

(a) [+2] For integers  $x, y, z$ , if  $x$  divides  $y$  and  $x$  divides  $z$ , then  $x$  divides  $y + z$ .

(b) [+2] For real numbers  $x, y$ , whenever  $x \geq y$ , it must be the case that  $x^2 \geq y^2$ .